Objectives O	Function Calls	Example Recursions O	Lists 00000	References O	Objectives •	Function Calls	Example Recursions O	Lists 00000	References O		
					Objectives						
		Basic Recursion									
	Dr. Mattox Beckman				<ul> <li>Diagram the stack frames that result from a series of function calls.</li> <li>Use HASKELL to write a recursive function on integers.</li> </ul>						
	University of Illinois at Urbana-Champaign Department of Computer Science				► Use F	ASKELL to write a recur	rsive function on lists.				

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## **Function Calls**

• Remember the syntax of a function definition in HASKELL.

#### Function Syntax

#### 1**foo** a =

- 2 let aa = a \* a
- ₃ in aa + a
- ► The above function has one paramater and one local.
- ► If we call it three times, what will happen in memory?

$$\mathbf{x} = (\text{foo } 1) + (\text{foo } 2) + (\text{foo } 3)$$

### Function Calls

• Remember the syntax of a function definition in HASKELL.

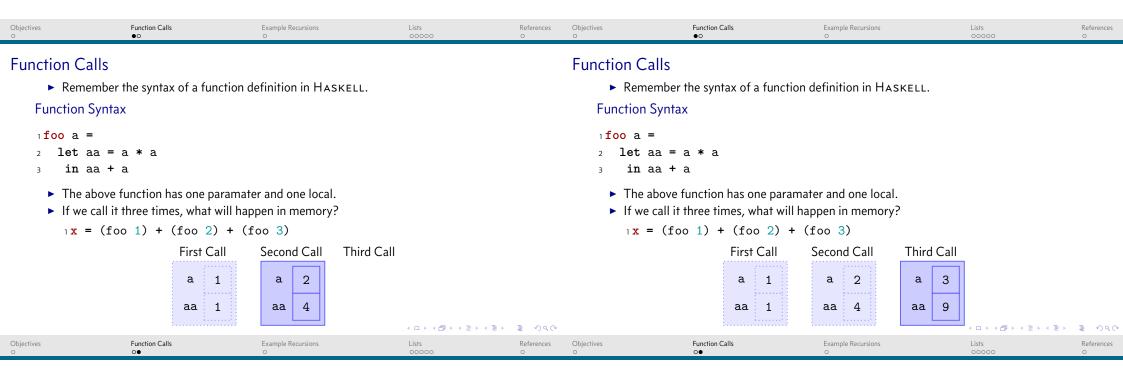
#### **Function Syntax**

1**foo** a = 2 **let** aa = a \* a

- 3 in aa + a
- The above function has one paramater and one local.
- If we call it three times, what will happen in memory?

$$1 \mathbf{x} = (foo \ 1) + (foo \ 2) + (foo \ 3)$$

First Call Second Call Third Call



### **Functions Calling Functions**

• If one function calls another, *both* activation records exist simultaneously.

```
1foo x = x + bar (x+1)
2bar y = y + baz (y+1)
3baz z = z * 10
```

► What happens when we call foo 1?

## **Functions Calling Functions**

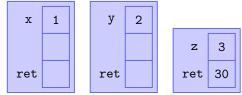
- ▶ If one function calls another, both activation records exist simultaneously.
  - 1 foo x = x + bar (x+1)
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    3 baz z = z \* 10
- ▶ What happens when we call foo 1?



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Functions Calling Functions					Functions Calling Functions						
•	If one function calls another, both a	activation records exist	t simultaneously.		•	If one function calls another,	, both activation records exist	simultaneously.			
	foo x = x + bar (x+1)					1 foo x = x + bar (x+1)					
	2 bar y = y + baz (y+1) 3 baz z = z * 10				$_{2}$ bar y = y + baz (y+1) $_{3}$ baz z = z * 10						
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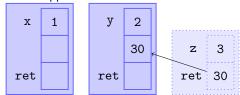
## Functions Calling Functions

- ► If one function calls another, *both* activation records exist simultaneously.
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## Functions Calling Functions

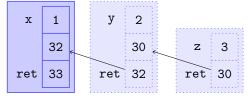
- ▶ If one function calls another, *both* activation records exist simultaneously.
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Objectives O	Function Calls ⊙●	Example Recursions O	Lists 00000		Objectives O	Function Calls ⊙●	Example Recursions O	Lists 00000	References O			
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▶	f one function calls another, bot	<i>h</i> activation records exist	simultaneously.		► If or	ne function calls another, b	ooth activation records exist	simultaneously.				
	foo $x = x + bar (x+1)$				1 foo x = x + bar (x+1)							
	<b>bar</b> $y = y + baz (y+1)$ <b>baz</b> $z = z * 10$				$_{2}$ bar y = y + baz (y+1) $_{3}$ baz z = z * 10							
		10										
	y   2     x   1   y   2     ret   30   ret   32	z 3 ret 30				at happens when we call for x 1 y 2 32 30 et ret 32	z 3 ret 30					
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# **Functions Calling Functions**

- ► If one function calls another, *both* activation records exist simultaneously.
  - 1 foo x = x + bar (x+1) 2 bar y = y + baz (y+1)3 baz z = z \* 10
- ► What happens when we call foo 1?



### Factorial

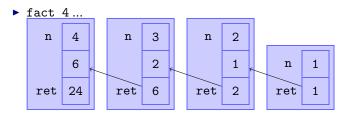
This works if the function calls itself.

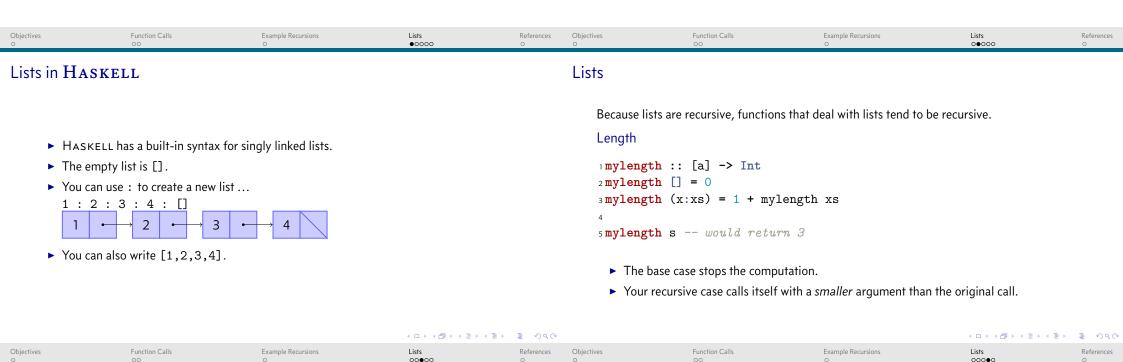
Factorial

1 fact 0 = 1

 $_{2}$  **fact** 1 = 1

 $\beta$  fact n = n \* fact (n-1)





Activity

#### Solutions to fib and sumList

- Write a function fib that computes the *n*th Fibonacci number  $F_n$ . Let  $F_1 = 1$  and  $F_2 = 1$ .
- Write a function sumList that takes a list and sums its elements.
- Write a function incList that takes a list and increments its elements.

```
1 fib 1 = 1
2 fib 2 = 1
3 fib n = fib (n-1) + fib (n-2)
4
5 sumList [] = 0
6 sumList (x:xs) = x + sumList xs
```

Objectives O	Function Calls	Example Recursions O	Lists 00000	References O	Objectives o	Function Calls	Example Recursions O	Lists 00000	References •	
Solution to incL	ist			History						

• Remember that you must create a new list!

incList [] = []
incList (x:xs) = x+1 : incList xs

• The first programming language to implement recursion was LISP in 1958. [McC79]

#### References

[McC79] John McCarthy. *History of Lisp*. Stanford University, 1979. URL: http://www-formal.stanford.edu/jmc/history/lisp.html.

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