

# Sum Types

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# Objectives

- ▶ Describe the syntax for declaring disjoint data types in HASKELL.
- ▶ Show how to use disjoint types to represent lists, expressions, and exceptions.
- ▶ Explain the operation and implementation of the list, Maybe and Either data types.
- ▶ Use a disjoint datatype to represent an arithmetic calculation.

# Simple Type Definitions

## Disjoint Type Syntax

```
data TName = CName [type ...] [| CName [type ...] ...]
```

A *sum type* has three components: a *name*, a set of *constructors*, and possible *arguments*.

```
1 data Contest = Rock | Scissors | Paper
2 data Velocity = MetersPerSecond Float
3               | FeetPerSecond Float
4 data List a = Cons a (List a)
5             | Nil
6 data Tree a = Node a (Tree a) (Tree a)
7             | Empty
```

## Example of Contest and Velocity

```
1 winner Rock Scissors = "Player 1"
2 winner Scissors Paper = "Player 1"
3 winner Paper Rock = "Player 1"
4 winner Scissors Rock = "Player 2"
5 winner Paper Scissors = "Player 2"
6 winner Rock Paper = "Player 2"
7 winner _ _ = "Tie"
8
9 thrust (FeetPerSecond x) = x / 3.28
10 thrust (MetersPerSecond x) = x
```

# The Most Fun Datatypes Are Recursive

## Our Own List Construct

```
1 data List = Cons Int List
2           | Nil
3   deriving Show
4 insertSorted a Nil = Cons a Nil
5 insertSorted a (Cons b bs)
6   | a < b      = Cons a (Cons b bs)
7   | otherwise = Cons b (insertSorted a bs)
```

We can run it like this:

```
*Main> let l1 = insertSorted 3 (Cons 2 (Cons 4 Nil))
*Main> l1
Cons 2 (Cons 3 (Cons 4 Nil))
```

## Type Constructors and Memory

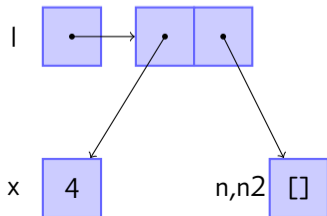
- ▶ When a type constructor is invoked, it causes memory to be allocated.
  - ▶ Writing an integer
  - ▶ Writing [] or Nil
  - ▶ Using : or Cons
- ▶ Writing down a variable does not cause memory to be allocated.

1 **x** = 4 -- allocates 4

2 **n** = [] -- allocates empty list

3 **n2** = n -- does NOT allocate memory

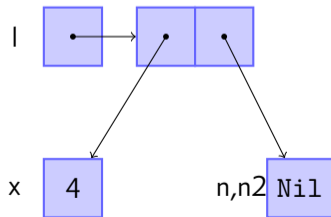
4 **l** = x:n -- A cons cell is allocated, but not the 4 or the empty list



## Similarly ...

```
1 x = 4
2 n = Nil
3 n2 = n
4 l = Cons x n
```

- ▶ Our own types do the same thing.



# Parameters

HASKELL supports *parametric polymorphism*, like templates in C++ or generics in JAVA.

## Parametric Polymorphism

```
1 data List a = Cons a (List a)
2           | Nil
3   deriving Show
```

```
1 x1 = Cons 1 (Cons 2 (Cons 4 Nil)) -- List Int
2 x2 = Cons "hi" (Cons "there" Nil) -- List String
3 x3 = Cons Nil (Cons (Cons 5 Nil) Nil) -- List (List Int)
```



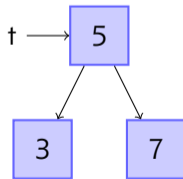
## BST Add

- ▶ Here is some code for BST Add!
- ▶ Note the dual use of a constructor: both for building and for pattern matching.

```
1 data Tree a = Node a (Tree a) (Tree a)
2             | Empty
3 add_bst :: Integer -> Tree Integer -> Tree Integer
4 add_bst i Empty = Node i Empty Empty
5 add_bst i (Node x left right)
6   | i <= x      = Node x (add_bst i left) right
7   | otherwise   = Node x left (add_bst i right)
```

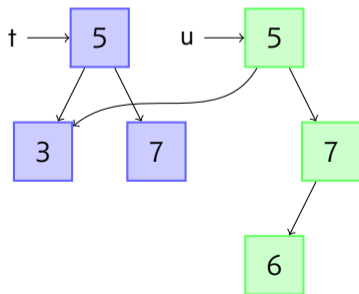
## Functional Updating

- ▶ It is important to understand functional updating.
- ▶ We don't update in place. We make copies, and share whatever we can.
  - ▶ Example: add 5,3,7 to a tree  $t$
  - ▶ `let u = add t 6`
  - ▶ `let v = add u 1`



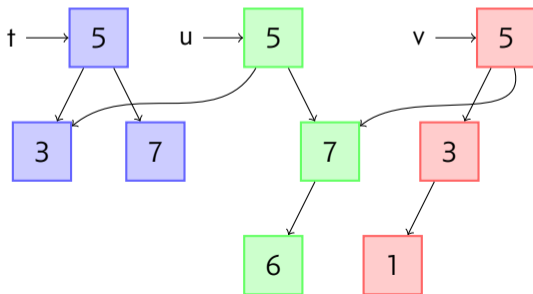
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# The Maybe Type

## The Maybe Type

```
1 data Maybe a = Just a | Nothing
```

Remember the lookup function that didn't know what to do if the item wasn't in the list?

```
1 getItem key [] = Nothing
2 getItem key ((k,v):xs) =
3     if key == k then Just v
4     else getItem key xs
```

Example:

```
*Main> getItem 3 [(2,"french hens"), (3,"turtle doves")]
Just "turtle doves"
*Main> getItem 5 [(2,"french hens"), (3,"turtle doves")]
Nothing
```

# The Either Type

## The Either Type

```
1 data Either a b = Left a | Right b
```

We can use it in places where we want to return something, or else an error message.

```
1 getItem key [] = Left "Key not found"
2 getItem key ((k,v):xs) =
3     if key == k then Right v
4     else getItem key xs
```

Example:

```
*Main> getItem 3 [(2,"french hens"), (3,"turtle doves")]
Right "turtle doves"
*Main> getItem 5 [(2,"french hens"), (3,"turtle doves")]
Left "Key not found"
```

## You try!

```
1 data Tree a = Branch a (Tree a) (Tree a)
2             | Empty
3 deriving Show
```

1. Write `add :: Tree a -> a -> Tree a`
2. Write `find :: Tree a -> a -> Bool`
3. Write `lookup :: Tree (k,v) -> k -> Maybe v`
4. Write `delete :: Tree a -> a -> Tree a`