

Objectives

State

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- ▶ Describe the property of *referential transparency*.
- ▶ Explain how stateful computations complicate the meaning of programs.
- ▶ Use OCAML's references to model state.

Definition

The rule of *referential transparency*:

$$\frac{e_1 \rightarrow^* v \quad e_2 \rightarrow^* v \quad f e_1 \rightarrow^* w}{f e_2 \rightarrow^* w}$$

- ▶ If you have two expressions that evaluate to be the same thing then you can use one for the other without changing the meaning of the whole program.
- ▶ E.g. $f(x) + f(x) == 2 * f(x)$
- ▶ You can prove this by induction, using the natural semantic rules from the previous lectures.

- ▶ You can use equational reasoning to make the following equivalence:

$$f(\text{if } e_1 \text{ then } e_2 \text{ else } e_3) \equiv \text{if } e_1 \text{ then } f(e_2) \text{ else } f(e_3)$$

```
1 x * (if foo then 20 / x else 23 / x) -- equivalent to
2 if foo then 20 else 23 -- well, mostly
```

- ▶ You have the basis now of many compiler optimization opportunities!

A Complication

```

1 # let counter = -- something
2 val counter : unit -> int = <fun>
3 # counter ();;
4 - : int = 1
5 # counter ();;
6 - : int = 2
7 # counter ();;
8 - : int = 3
9 #

```

- ▶ Can we still use equational reasoning to talk about programs now?

Reference Operator

Transition Semantics

$\text{ref } v \rightarrow \i , where $\$i$ is a free location in the state, initialized to v .

$! \$i \rightarrow v$, if state location $\$i$ contains v .

$\$i := v \rightarrow ()$, and state location $\$i$ is assigned v .

$() ; e \rightarrow e$

Note that references are different than pointers: once created, they cannot be moved, only assigned to and read from.

A Counterexample

▶ $f(x) + f(x) == 2 * f(x)$

```

1 # 2 * counter ();;
2 - : int = 8
3 # counter () + counter ();;
4 - : int = 11

```

▶ Congratulations. You just broke mathematics.

Natural Semantics

$\frac{e \Downarrow v}{\text{ref } e \Downarrow \$i}$, where $\$i$ is a free location in the state, initialized to v .

$\frac{e \Downarrow \$i}{!e \Downarrow v}$, if state location $\$i$ contains v .

$\frac{e_1 \Downarrow \$i \quad e_2 \Downarrow v}{e_1 := e_2 \Downarrow ()}$, and location $\$i$ is set to v .

$\frac{e_1 \Downarrow () \quad e_2 \Downarrow v}{e_1 ; e_2 \Downarrow v}$

Counter, Method 1

```
1 # let ct = ref 0;;
2 val ct : int ref = {contents=0}
3 # let counter () =
4   ct := !ct + 1;
5   !ct;;
6 val counter : unit -> int = <fun>
7 # counter ();;
8 - : int = 1
9 # counter ();;
10 - : int = 2
```



Conclusions about State

State is bad because:

- ▶ It breaks our ability to use equational reasoning.
- ▶ Users can get to our global variables and change them without permission.

State is good because:

- ▶ Certain constructs are almost impossible without state (e.g., graphs).
- ▶ Our world is a stateful one.



Bad Things for Counter

ct is globally defined. Two bad things could occur because of this.

1. What if you already had a global variable ct defined?
 - ▶ Correct solution: use modules.
2. The Stupid UserTM might decide to change ct just for fun.
 - ▶ Now your counter won't work like it's supposed to!
 - ▶ Now you can't change the representation without getting tech support calls.
 - ▶ Remember the idea of *abstraction*.

